## INSTITUTE OF ACTUARIES OF INDIA

## EXAMINATIONS

$14^{\text {th }}$ September 2017

## Subject ST7 - General Insurance: Reserving and Capital Modeling

## Time allowed: Three Hours (14.45* - 18.00 Hours)

Total Marks: 100
INSTRUCTIONS TO THE CANDIDATES

1. Please read the instructions inside the cover page of answer booklet and instructions to examinees sent along with hall ticket carefully and follow without exception.
2.     * You have 15 minutes at the start of the examination in which you are required to read the questions. You are strongly encouraged to use this time for reading only, but notes may be made. You have then three hours to complete the paper.
3. You must not start writing your answers in the answer sheet unless instructed to do so by the supervisor.
4. The answers are not expected to be any country or jurisdiction specific. However, if Examples/illustrations are required for any answer, the country or jurisdiction from which they are drawn should be mentioned.
5. Attempt all questions, beginning your answer to each question on a separate sheet.
6. Mark allocations are shown in brackets.
7. Please check if you have received complete Question paper and no page is missing. If so, kindly get a new set of Question paper from the Invigilator.

Please return your answer book and this question paper to the supervisor separately.
Q. 1) XYZ is a medium size insurance company and has been in business for many years. The company has well managed data systems which capture various product and claims details appropriately.

The actuary has been assigned the task to build a stochastic capital model for the company which covers all the major risks faced by the company.
i) Discuss the various challenges faced by the actuary with regards to data limitations. For each of these, discuss possible measures that could be taken to improve the correctness of the capital model.
ii) Discuss various checks that can be performed to validate the results of the model.
Q. 2) The actuary of $A B C$ general insurance has two options to estimate company's net reserves:
a) Estimate gross reserves using gross claims triangles and then net them down using various gross to net ratios.
b) Estimate net reserves using net claims triangles directly.
i) Discuss the pros and cons of the two approaches.
ii) Discuss another three alternative approaches which could be used to model net claims.
Q. 3) i) The records maintained by various police stations in the country were manual till now. The Government has decided to digitize the records and details of records could be fetched from any police station nationwide. Discuss the impact of digitization of police records on the claim reserves.
ii) Recently 3-year motor third party insurance contracts have been allowed by the regulator. The premium charged under such contract is 3 times the yearly premium prescribed by the tariff. Discuss the impact on:
a) Calculation of the earning of premium for such contract.
b) Investment strategy of the company.
Q. 4) A general insurance company is thinking of launching jewelry insurance cover.
i) Discuss possible coverage offered under this product including the list of perils.
ii) List the various rating factors for the product.
iii) State various ways to reduce the likelihood of moral hazard under this product.
iv) Suggest suitable reinsurance arrangements for the product
v) How the product is likely to impact the Profit and loss statement of the company in various years.
Q. 5) i) The frequency and severity underlying an insurance product varies by the quarter of the year and is shown in the table below ( x and y represent the base frequency and severity
respectively). Assuming no expenses or acquisition costs and that pricing is adequate and reflects quarterly earning pattern, what is the UPR for a
a) 1 year policy written on January $1^{\text {st }}$ at the end of Q2.
b) 6 month policy written on July $1^{\text {st }}$ at the end of Q3.

| Quarter | Frequency | Severity |
| :---: | :---: | :---: |
| 1 | x | 2 y |
| 2 | 0.75 x | 2 y |
| 3 | 0.5 x | y |
| 4 | 0.25 x | y |

ii) Provide arguments against closing down an insurance company on the basis of an operating ratio recorded in excess of $100 \%$ implying failure to achieve satisfactory levels of profit.
Q. 6) As the appointed actuary of an insurance company, you have been requested by the board to evaluate the different reinsurance options available to the company. Provide a report for the board addressing the following three items
i) The factors affecting an insurer's appetite for offsetting its risks through reinsurance
ii) Fronting and the reasons for choosing it
iii) Facultative reinsurance and its advantages and disadvantage
Q. 7) You are given the following cumulative paid loss triangle.

| Cumulative Paid Losses (INR Crores) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 12 | 24 | 36 | 48 | 60 |
| 2012 | 2400 | 7600 | 10500 | 13000 | 14500 |
| 2013 | 2300 | 7250 | 9750 | 12000 |  |
| 2014 | 2100 | 6500 | 8600 |  |  |
| 2015 | 2000 | 6000 |  |  |  |
| 2016 | 1900 |  |  |  |  |

i) Calculate the triangle of link-ratios (and the all-year volume weighted average link ratio) and estimate the unpaid liability.

Based on your request for further information, you are given the triangle of cumulative closed claims and the estimated ultimate reported claims.

## Cumulative Closed Claims

|  | 12 | 24 | 36 | 48 | 60 | Ult. Reported Claims |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2012 | 4056 | 6552 | 7098 | 7566 | 7792 | 7800 |
| 2013 | 4386 | 7052 | 7654 | 8256 |  | 8600 |
| 2014 | 4851 | 7821 | 8613 |  |  | 9900 |
| 2015 | 4512 | 7296 |  |  |  | 9600 |
| 2016 | 4050 |  |  |  |  | 9000 |

ii) Calculate the claim disposal ratios and comment on its pattern
iii) Restate the cumulative closed claims per the Berquist-Sherman method using the latest diagonal of disposal rates as representative
iv) Calculate the Berquist-Sherman adjusted paid loss triangle based on the following additional information.
a) Cumulative Paid Losses $=Y$
b) Restated Cumulative Closed Claims $=X$ (as per (iii) above)
c) You have fit the exponential curve $\mathrm{Y}=\mathrm{a}^{*} \exp \left(\mathrm{~b}^{*} \mathrm{X}\right)$ to each year of the triangle and the coefficients are given below

|  | a | b |
| :---: | :---: | :---: |
| 2012 | 335.97 | 0.000483 |
| 2013 | 347.24 | 0.000429 |
| 2014 | 339.12 | 0.000375 |
| 2015 | 337.1 | 0.000395 |

v) Calculate the Berquist-Sherman Reserve for the adjusted paid loss triangle (use all-year volume weighted averages for linked ratios)
vi) Would you include the claim disposal rate as a source of uncertainty in your actuarial "best estimate" and range communication? Why or why not?
Q. 8) i) You are given the following -
a) The number of claims for a line in a year follow the following distribution

| $\#$ | Prob. |
| :---: | :---: |
| 0 | $60 \%$ |
| 1 | $20 \%$ |
| 2 | $20 \%$ |

b) The amount of each claim for the line in a year follows the following distribution

| Amount | Prob. |
| :---: | :---: |
|  |  |
| 10,000 | $80 \%$ |
| 100,000 | $20 \%$ |

An insurer and a reinsurer have an annual aggregate excess of loss agreement with limit $=$ 50,000 for all claims arising from this line.

What is the copula function for the joint distribution of aggregate annual payout of the insurer and reinsurer?
ii) The following methods have been suggested for adjusting reserves to allow for reserve risk:
a) Reserves are set equal to the best estimate plus $10 \%$
b) Reserves are set equal to the $75^{\text {th }}$ percentile amount
c) Reserves are set equal to the best estimate plus one standard deviation

Describe the rationale behind each approach and outline briefly the advantages and disadvantages of each method.

